Enrollm	nent No: Exam Seat No:		
	C.U.SHAH UNIVERSI	ГҮ	
	<b>Summer Examination-201</b>	.7	
Subject 1	Name: Numerical Methods		
Subject	Code: 4SC04MTE1 Branch: B.Sc.(Ma	athematic	es,Physics)
Semester	er: 4 Date: 20/04/2017 Time: 10:30 To 0	Time: 10:30 To 01:30 Mar	
(2) I (3) I	Use of Programmable calculator & any other electronic instrur Instructions written on main answer book are strictly to be obe Draw neat diagrams and figures (if necessary) at right places. Assume suitable data if needed.  Attempt the following questions		(14)
<b>a</b> )	The method has a fast rate of convergence.  (a) Bisection method (b) False position method (c) Newton Raphson method (d) none of these	thod	(01)
<b>b</b> )	The modified Euler's method is the Runge-Kutta method of (a) 3 <sup>rd</sup> (b) 1 <sup>st</sup> (c) 4 <sup>th</sup>		der. (01)
c)	Out of four Runge-Kutta methods, the Runge-Kutta method commonly used in applications.  (a) 3 <sup>rd</sup> (b) 1 <sup>st</sup> (c) 4 <sup>th</sup>	of or (d) 2	
d)	Write Picard's formula for $\frac{dy}{dx} = f(x, y)$ with $f(x_0) = y_0$ .		(01)
e) f) g) h) i)	What is the value of $f'(x)$ in general by Stirling inter polatic Write Simpson's one third rule.  Write $n^{th}$ approximation of iteration method.  Give value of $f'''(x)$ by Newton's forward interpolation for Give general formula for Modified Euler Method.		a? (01) (01) (01) (01) (02)

- j) Give value of a & b such that root of f(x) = 0 lies between a & b, where  $f(x) = x^2 + x 5$ . (02)
- k) Find the value of  $\int_0^1 e^x dx$  with h = 1/2 by Trapezoidal rule. (02)

## Attempt any four questions from Q-2 to Q-8.

Q-1

Q-2 Attempt all questions

a) Find the positive root of 2x = 3 + cos x by bisection method.
b) Find a root of f(x) = 3x - 6 - log<sub>10</sub> x using Iteration Method up to four decimal places.
c) Find a root of the equation x³ - 2x - 5 = 0 correct up to three significant figures by using the Newton-Raphson method.

(05)
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(06)



Q-3		Attempt all questions	(14)
	a)	Evaluate $\int_{0}^{6} \log x  dx$ by Weddle's rule and taking n=5.	(05)
	<b>b</b> )	Evaluate $\int_{0.1}^{2} e^x + 2x  dx$ by Trapezoidal rule and taking n = 6.	(05)
	c)	Evaluate $\int_{0}^{\frac{\pi}{2}} e^{\sin x} dx$ by Simpson's 3/8 rule and taking n = 6.	(04)
Q-4	a)	Attempt all questions Prove that Newton-Raphson Method has second order convergence.	(14) (05)
	b)	Apply Taylor's series method to obtain approximate value of $y$ at $x = 0.2$ for the differential equation $\frac{dy}{dx} = 2y + 3e^x$ , $y(0) = 0$ .	(05)
	c)	Find a root of the equation $\cos x - xe^x = 0$ correct up to three decimal places by using the False-position method.	(04)
Q-5	a)	Attempt all questions Find the solution of $\frac{dy}{dx} = e^x - y$ up to the fifth approximation. Using Picard's method given that $y(0) = 0$ .	(14) (07)
	<b>b</b> )	Apply Milne's method to find the solution of the differential equation $\frac{dy}{dx} = x - y^2$ in the range $0 \le x \le 1$ .	(07)

## Q-6 Attempt all questions

(14) (07)

Find $f'(0)$ from the following data:						
x	3	5	11	27	34	
f(x)	-13	23	899	17315	25606	

**b**) Derive f'(x) by Newton's Forward Interpolation Formula.

**(07)** 

## Q-7 Attempt all questions

**(14)** 

a) Determine y(0.1) and y(0.2) correct to four decimal places from  $\frac{dy}{dx} = 2x + y$ , y(0) = 1. Use fourth order Runge-Kutta method. (07)

**b)** Using Euler modified method, obtain a solution of  $\frac{dy}{dx} = x + |\sqrt{x}|$ , y(0) = 1 for the range  $0 \le x \le 0.6$  in steps of 0.2.



## Q-8 Attempt all questions

(14) (07)

(07)

a) Find the value of f'(0.5) and f''(0.5) using Stirling's formula from the following data

x	0.35	0.40	0.45	0.50	0.55	0.60	0.65
у	1.521	1.506	1.488	1.467	1.444	1.418	1.389

**b)** The table given below reveals the velocity v of a body during the time t specified. Find its acceleration at t = 1.1

D	specified. This its deceleration at $t=1.1$							
	t	1.0	1.1	1.2	1.3	1.4		
ſ	v	43.1	47.7	52.1	56.4	60.8		